Inverse design of plasmonic metasurfaces by convolutional neural network

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Artificial neural networks have shown effectiveness in the inverse design of nanophotonic structures; however, the numerical accuracy and algorithm efficiency are not analyzed adequately in previous reports. In this Letter, we demonstrate the convolutional neural network as an inverse design tool to achieve high numerical accuracy in plasmonic metasurfaces. A comparison of the convolutional neural networks and the fully connected neural networks show that convolutional neural networks have higher generalization capabilities. We share practical guidelines for optimizing the neural network and analyzed the hierarchy of accuracy in the multi-parameter inverse design of plasmonic metasurfaces. A high inverse design accuracy of ±8 nm for the critical geometrical parameters is demonstrated. © 2020 Optical Society of America

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The deep neural networks (DNNs) have been proven to be powerful in solving complicated problems in various fields ranging from biology [1], chemistry [2], physics [3], to geology [4]; and from theoretical calculations [5] to engineering applications [6]. In the field of nanophotonics [7], the DNNs have been employed to design plasmonics structures, metasurfaces [8], integrated photonic devices [9], and nanocavities [10]. The popularity of the DNNs stems from the fact that they can handle complex problems requiring high scientific rigor and precision. Instead of expressing and solving the physical equations in an explicit way, the DNNs can extract the physics hidden in the statistics of data and memorize them as network parameters through the learning process. In principle, the DNNs can approximate any physical phenomenon, provided that the capacity is high enough. However, the tuning of the DNNs is a nontrivial task. The performance of the DNNs is highly sensitive to the training data, DNN architecture, hyperparameter tuning, and regularization techniques. All these aspects have to be considered before applying the DNNs to a specific problem.

Localized surface plasmons (LSPs) of metals are immensely important for applications such as surface-enhanced spectroscopy [11,12], sensing [13,14], optoelectronic devices [15–17], and imaging [18,19]. The aggregation of plasmonic nanostructures gives rise to rich physics phenomena including Fano resonances [20,21] and complicated hybridization [22,23]. Harnessing the power of the coupling LSPs can enable designs of optical structures with an on-demand spectral response. Conventionally, such a task requires a deep understanding of the physics by solving Maxwell’s equations using finite-difference time-domain (FDTD) and finite-element method (FEM). The design methods typically comprise the sweeping of parameters and trial and error. While this is not so difficult in a simple symmetric system with fewer parameters, the challenge grows exponentially as the problem becomes asymmetric and complex [24]. For instance, the unit cell considered here can be described by six parameters, which means searching for the optimal value in a six-dimensional space. Since the unit cell size is sub-wavelength, the coupling between the unit cells has to be considered, making the system design more complicated. Recently, there is a growing interest in tackling these problems using fully connected (FC) DNNs [9,24–27] and convolutional neural networks (CNN) [28]. However, a comparison of these two types of structures in the photonics inverse design problem is still lacking. Moreover, the numerical accuracy of neural networks in the multi-parameter inverse design problem has not been addressed adequately in the previous reports.

In this work, we demonstrate that convolutional neural networks (CNNs) are significantly better in the inverse design of plasmonic metasurfaces based on a target spectrum. The advantages are two-fold. First, since the starting point of such an inverse design problem is usually a target spectrum where the valleys and the peaks are the defining features, the CNNs can extract these features and perform analysis on them, a process which has been extensively demonstrated in image recognition [29]. In this sense, the CNNs yield more accountability for the inverse design process. Second, the connections of the CNNs are sparse [30]; namely, only a small patch of neurons are connected to the previous layer. It is a way to remove the redundant information, thus reducing the difficulty in training and improving both accuracy and generalization capabilities [31]. In the inverse design problem based on the spectral response, the peaks and valleys are the main important information. The CNNs can take advantage of this and allow for more accurate and robust inverse design.

We consider a plasmonic metasurface whose unit cell consists of three gold (Au) nanodisks as shown in Fig. 1(a). The fabrication process is as follows. First, a layer of Au (50 nm) is deposited on a double-side polished sapphire substrate by sputtering;
square unit cell. (c) Illustration of how the symmetry of the structure can cause data inconsistency.

Fig. 1. (a) SEM image of the fabricated plasmonic metasurface, and the scale bar is 1 μm. (b) Schematic of geometrical parameters of the square unit cell. (c) Illustration of how the symmetry of the structure can cause data inconsistency.

Fig. 2. Detailed parameters of the CNN.

subsequently, the photoresist is spin-coated on the substrate and electron-beam lithography is used to write the pattern. After developing, the Au is etched by inductively coupled plasma etching (ICP) with the photoresist as the etching mask. Six parameters can be defined to fully describe the geometry of a unit cell. They are the diameters of the three disks p1, p2, p3, the inter-disk distances p4, p5, and the angle p6 as shown in Fig. 1(b). Previously, stand-alone plasmonic trimer systems have been shown to exhibit rich physics phenomena by virtue of the interactions between the plasmonic nanoparticles [22,32,33].

An illustration of the detailed network structure can be found in Fig. 2. It is comprised of convolutional layers (Conv1D) and linear layers. The input data of the neural network are the input data of the CNN as the loss function during training and as the error function during validation. The loss function is minimized by gradient descent using the Adam optimization algorithm [30] in the training process. The learning rate is set as 0.01 initially, and it is dropped by a factor of 1.2 every 50 epochs. The training sets are fed to the network with batch sizes of 100. The training and validation losses are obtained by a 5-fold cross-validation procedure and are shown in Figs. 3(a) and 3(b). To make a comparison between the CNNs and FC DNNs, another model that consists of only linear layers is built. In the FC DNN structures, the convolutional layers are replaced by three linear layers with the node numbers of 300, 900, and 2200, respectively. The ReLu and BN layers are maintained after each linear layer. The parameters are chosen based on the considerations to make the FC DNN network balanced. However, the total trainable parameters of these three layers alone are 2.25 × 10^6, in contrast, the total trainable parameters of the Conv1D layers are 1260. We compare the CNN and FC DNN with and without batch normalization in Fig. 3. A few sharp drops in Fig. 3(a) can be discerned at epochs 100, 150, and 200 due to the learning rate modulation, which shows that the modulation of the learning rate is helping to accelerate the training process.
training process for different neural network architectures. p2, and p3 follow the trend of y and approximate peak and valley positions. The predicted p1, important parameters defining the overall shapes of the spectra the diameter of the three nanodisks. Hence, they are the most p4, p5, and p6 is lower. The parameters p1, p2, and p3 have the highest accuracy while the accuracy of = y ± 8, respectively, are plotted as guidelines. We = x ± 8 nm. The = x, and the red lines represent y = x ± 8. Without the batch normalization layers, the training loss decreases continuously to almost zero while the validation loss starts increasing after 100 epochs for both FC DNN and CNN, which is a clear sign of overfitting [34]. However, with the addition of the batch normalization layers, both the training and validation loss stabilized to a relatively low value, which indicates the batch normalization layers are helping to prevent overfitting in both CNN and FC DNN. The comparison of the FC DNN and the CNN is shown by the purple and cyan curves in Figs. 3(a) and 3(b). The training loss in Fig. 3(a) for both CNN and FC DNN converge to the same level, which indicates that both are well-trained and have the capability to fit training data well. However, the validation loss of the FC DNN is twice higher than that of CNN, indicating poor generalization capabilities, which can be attributed to the dense connections of FC DNN [31,35,36].

After the CNN is trained, the spectra in the testing set are fed to it and the predicted parameters p1-p6 are compared with the initial values used to generate the spectra. Figure 4 shows the comparison. The black and red dashed lines representing y = x and y = x ± 8, respectively, are plotted as guidelines. We observe there is a hierarchy in the accuracy. The parameters p1, p2, and p3 have the highest accuracy while the accuracy of p4, p5, and p6 is lower. The parameters p1, p2, and p3 decide the diameter of the three nanodisks. Hence, they are the most important parameters defining the overall shapes of the spectra and approximate peak and valley positions. The predicted p1, p2, and p3 follow the trend of y = x closely and with 90% of the points fall within the boundaries of y = x ± 8 nm. The parameters p4, p5, and p6 are related to the coupling strength between disks, and therefore they are parameters to fine-tune the spectrum. The parameter p5 has the lowest accuracy with the maximum deviation as high as 40 nm. This is because the parameter p5 controls the coupling between d1 and d2, which is weak in this work since the polarization direction is largely perpendicular to the coupling axis. On the contrary, the parameter p4 controls the coupling between d1 and d3, and the polarization is not always perpendicular to the coupling axis due to the rotation of p6. Thus the accuracy of p4 is higher. This point will be addressed in detail in the following paragraphs. The hierarchy of the accuracy is an indication that the network is learning the importance of each parameter p1-p6.

To further evaluate the performance of the proposed approach, an arbitrary spectrum modified from the testing data set with three plasmonic resonance peaks [the purple curve in Fig. 5(a)] is fed to the CNN. Afterward, an FDTD simulation is carried out using the predicted parameters p1-p6 to get the absorption spectrum. The comparison between the target spectrum and the one obtained from the network geometry (the green curve) is shown in Fig. 5(a). There are three peaks in the target spectrum at 680, 875, and 1225 nm, which are all well fitted by the network predicted parameters. Figure 5(b) shows the parameters p1-p6 predicted by the CNN. The metasurface is fabricated based on these parameters [Fig. 1(a)], and the absorption spectrum [Fig. 5(a)] is measured by a VIS/NIR spectrophotometer with a polarizer. There are some shifts and broadening of the resonant peaks, which are mainly due to the errors of the fabrication of small feature sizes down to 50 nm. However, the overall resonant peak positions marked by black arrows agree well with the prediction by the CNN. To investigate the origin of each plasmonic peak, we plot the charge distribution and normalized electric field intensity distribution at the peak wavelengths in Figs. 5(c)–5(f). The electric field direction is generally horizontal due to the polarization of the incoming light [Fig. 5(c)]. Due to the hybridization of each plasmonic mode, we observe the antibonding mode at 680 nm and bonding mode at 1225 nm. At 875 nm, d1 shows quadrupole modes due to the coupling with d3. We observe that the electric field is much weaker between d1 and d2 compared to d1 and d3. This is because the incident light is almost perpendicular to the axis of d1 and d2, which results in reduced coupling strength...
Consequently, the parameter p5 has a higher error with deviations up to 40 nm.

On the contrary, the interaction between d1 and d3 is more prominent, as observed from the enhanced field between d1 and d3 in Figs. 5(c)–5(f). This could be attributed to the smaller size of d3 and the fact that the polarization is parallel to the axis of d1 and d3. However, the rotation of d3 is controlled by p6, and there are situations where the axis between d1 and d3 are almost perpendicular to the polarization direction, such as the case shown in Fig. 2(b). In these situations, the accuracy of p4 should deteriorate, however, we observe the accuracy of p4 is consistently high. This is because the coupling between p2 and p3 become prominent when p6 is small, thus p4 is still a critical parameter. Despite the deviations of p5 and p6, the overall accuracy is adequate, considering the deviation of ±8 nm of the critical geometrical parameters p1, p2, and p3 is merely 1.5% of the shortest wavelength in this study (600 nm) and similar to the resolution limit of state-of-the-art nanofabrication techniques.

In conclusion, we demonstrate the CNN as an excellent tool to achieve high accuracy inverse design of plasmonic metasurfaces. The superiority stems from the fact that it can recognize the peaks and valleys of a spectrum and it is computationally less costly. We also show that batch normalization can improve the performance of the CNN. A high design accuracy of ±8 nm is achieved for the critical geometrical parameters. Analysis of the results suggests the critical geometrical parameters possess significantly smaller errors than the less important ones. The technique and methodology can be applied to other inverse designs of nanophotonics involving target spectra.

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